

KAMONYI DISTRICT

HOLIDAYS WORK, 2024-2025

SUBJECT: MATHEMATICS II

-MATH-ECONOMICS-GEOGRAPHY (MEG)

-MATHEMATICS –COMPUTER-ECONOMY (MCE)

INSTRUCTIONS:

This paper has THREE sections A and B

SECTION A: Attempt ALL questions (55 marks)

SECTION B: Attempt any THREE questions (45 marks)

SECTION A: Attempt all the questions (55 marks)

1) Given the complex number $z = 45i$ $w = 7i - 10$

a) Complete the following table /2marks(0.5mark each)

Complex number	Real part	Imaginary part
Z		
W		

b) answer true or false/ 2marks (1mark each)

i) z is purely imaginary

ii) w is real

2) find the value of i^{2243} /2marks

3) calculate the following limits $\lim_{x \rightarrow 0} \frac{\ln(\cos x)}{x}$ /2marks

4) find the domain of definition of $f(x) = \ln \frac{x+1}{x-1}$ /4marks

5) find the monthly payment on a mortgage of 75000 frw on 8% interest rate that run for 20years /3marks

6) given $f(x) = \ln(1 - x)$ and $g(x) = e^x$

a) write the Maclaurin polynomial of degree three of $f(x)$ /2marks

b) write the Maclaurin polynomial of degree three of $g(x)$ /2marks

c) use the results obtained on a) to solve $\ln(1 - x) + e^x = 1$ /2marks

7) evaluate $\int (\sin 4x)e^{\cos 4x} dx$ /2marks

8) The population of a colony of rabbits in a park increases at a rate proportional to the population. Initially, there were ten rabbits in the park. When the population is 100 rabbits, the colony is increasing at a rate of seven rabbits per month.

a) Form a differential equation for the population increase and solve it./4marks

b) find the number of rabbits when $t=20$ months /1mark

9) Consider $F = \{(2x, 0, z): x, z \in \mathbb{R}\}$ and $G = \{(2x, 3y, 0): x, y \in \mathbb{R}\}$. . Verify Grassmann's formula of dimensions./4marks

10) find $\frac{dy}{dp}$ given that $y = \ln(p + \cos 2p)$ /3marks

11) use complex number to solve $\cos x + \sqrt{3}\sin x = \sqrt{3}$ /3marks

12) for all natural n, the numerical function $H_n(x) = \frac{x^n}{1+x^2}$, $x \in \mathbb{R}$, given

$M_n = \int_0^1 H_n(x) dx$ show that $\forall k \in \mathbb{N}$, $M_{2k} + M_{2k+1} = \frac{1}{2k+1}$ /4marks

13) a) linearise $\cos^2 8x \sin 3x$ /4marks

b) deduce $\int \cos^2 8x \sin 3x dx$ /2marks

14) find the general solution of the following differential equation:

$(1 + e^x) \frac{dy}{dx} = e^x$ /4marks

15) Let U and W be the following subspaces of \mathbb{R}^4 : $U = \{(a, b, c, d) : b + c + d = 0\}$
 $W = \{(a, b, c, d) : a + b = 0, c = 2d\}$. Find the dimension of $U \cap W$ /3marks

SECTION B: Attempt any 3 the questions (45 marks)

16) solve $y'' - 2y' = x + 2e^x$ given that $y(0) = 0, y'(0) = 1$ /15marks

17) given $I = \int_0^{\frac{\pi}{4}} (2x + 1)\cos^2 x dx$

And $M = \int_0^{\frac{\pi}{4}} (2x + 1)\sin^2 x dx$

a) calculate $I + M$ /2MARKS

b) calculate $I - M$ /8MARKS

C) deduce the value of I and M /5MARKS

18) using integration Find the length of the circle of radius H and centre $(0,0)$ /15MARKS

19) Let f be the linear transformation from \mathbb{R}^2 to \mathbb{R}^3 defined by $f(\vec{V}) = A\vec{V}$ with

$$A = \begin{pmatrix} 1 & 3 \\ 2 & 6 \\ 3 & 9 \end{pmatrix}$$

a) Find a basis for $\text{Ker}(f)$ /6Marks

b) Determine if f is one to one. /1Mark

c) Find a basis for the range of f /6Marks

d) Determine if f is onto /2Marks

20) given $p(z) = z^4 - 4(1 + i)z^3 + 12iz^2 - 8i(1 + i)z - 5$

a) Factorize completely $p(z)$ /10MARKS

b) Solve $p(z) = 0$ /5MARKS

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